

PROBLEMA 1:

$$(a) \quad f_i(t) = f_c + K_f m_1(t) = f_c + K_f \text{sinc}(320 \cdot 10^3 t)$$

Valor máximo:

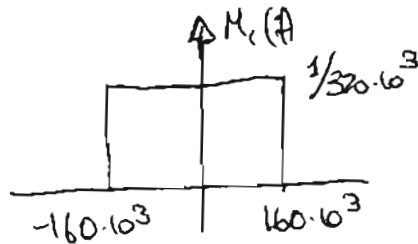
$$\boxed{f_i(t) \Big|_{\max} = f_c + K_f m_1(t) \Big|_{\max} = f_c + K_f \cdot 1 = 25 \cdot 10^6 \text{ Hz} + 240 \cdot 10^3 \text{ Hz/V} \cdot 1 \text{ V} = \boxed{25,24 \text{ MHz}}$$

$$B_T [\text{CARSON}] = 2\Delta f \left(1 + \frac{1}{D}\right)$$

$$\Delta f = K_f \cdot m_1(t) \Big|_{\max} = 240 \text{ KHz}$$

$$D = \frac{\Delta f}{W}$$

$$m_1(t) = \text{sinc}(320 \cdot 10^3 t) \quad \longleftrightarrow \quad \frac{1}{320 \cdot 10^3} \Pi \left(\frac{f}{320 \cdot 10^3} \right)$$



$$W = 160 \text{ KHz}$$

$$D = \frac{240 \text{ KHz}}{160 \text{ KHz}} = 1.5$$

$$\boxed{B_T [\text{CARSON}] = 2 \cdot 240 \cdot 10^3 \left(1 + \frac{1}{1.5}\right) = \boxed{800 \text{ KHz}}$$

$$\frac{B_T}{\Delta f} = \frac{2n_{\max}}{D}$$

$$\text{PARA } D=1 \Rightarrow n_{\max} = 3 \quad \frac{2n_{\max}}{D} = 6$$

$$D=2 \Rightarrow n_{\max} = 4 \quad \frac{2n_{\max}}{D} = 4$$

$$\text{INTERPOLANDO: } D=1.5 \quad \frac{2n_{\max}}{D} = 5$$

$$B_T [1\%] = \frac{2n_{\max} \cdot \Delta f}{D} = \cancel{5 \cdot 240 \text{ KHz}} \quad 5 \cdot 240 \text{ KHz} = 1200 \text{ KHz}$$

$$B_T = \frac{B_T [\text{CARSON}] + B_T [1\%]}{2} = 1 \text{ MHz}$$

(b) LA CONDICION: $P_c = \frac{A_c^2}{2} \geq 20 B_T N_0$

$$\frac{A_c^2}{N_0} \geq 40 B_T \Rightarrow A_c \geq \sqrt{40 B_T N_0} = 6325 \sqrt{N_0}$$

(c) $\text{SNR}_I = 30 \text{ dB} = 1000 = \frac{A_c^2}{2 N_0 B_T}$

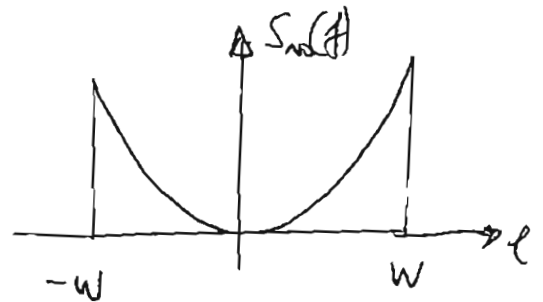
$$A_c^2 = 2000 B_T N_0 \Rightarrow$$

$$A_c = 44721 \sqrt{N_0}$$

SI SE CUMPLE CONDICION APARTADO (b), EL SISTEMA FUNCIONA POR ENCIMA DEL UMBRAL.

(d) LA DENSIDAD ESPECTRAL DE RUIDO A LA SALIDA:

$$S_{nb}(f) = \frac{N_0 f^2}{A_c^2} k^2 \Pi\left(\frac{f}{2W}\right)$$



SE HA AÑADIDO EL FACTOR k^2

$W = 160 \text{ KHz}$ ES EL ANCHO DE BANDA DE LA SEÑAL FDM.

CUANTO MAS ALEJADOS DEL ORIGEN MAS RUIDO, EL PRIMER CANAL MENOS RUIDO.

CANAL 1 0 A 4 KHz

PROBLEMA 1 (CONTINUA CON)

$$P_{No}^{\text{CANAL 1}} = 2 \int_0^{4000} S_{No}(f) df = 2 \frac{N_0}{A_c^2} k_d^2 \frac{f^3}{3} \Big|_0^{4000} =$$

$$= \frac{2 \cdot (10^{-6} \text{ V/Hz})^2 \cdot (4000)^3}{3 \cdot 2000 \cdot 10^6} = 2,13 \cdot 10^{-11} \text{ W}$$

(e) EL CANAL FDM MAS ALEJADO DEL ORIGEN DE FRECUENCIAS TENDRA MAS RUIDO: CANAL 40.

$$P_{No}^{\text{CANAL 40}} = 2 \int_{39.4000}^{40.4000} S_{No}(f) df = 2 \frac{N_0}{A_c^2} k_d^2 \frac{f^3}{3} \Big|_{156000}^{160.000}$$

$$= \frac{2 \cdot (10^{-6})^2 [(160 \cdot 10^3)^3 - (156 \cdot 10^3)^3]}{3 \cdot 2000 \cdot 10^6} = 9,99 \cdot 10^{-8} \text{ W}$$

$$SNR_0 = \frac{3 A_c^2 k_d^2 P}{2 W^3 N_0} = \frac{3 \cdot (240 \cdot 10^3)^2 \cdot 1 \cdot 2 \cdot 10^9}{2 \cdot (160 \cdot 10^3)^3} = 42187,5 = 46,25 \text{ dB}$$

$$P_{No}^{\text{Total}} = 2 \int_0^{40.4000} S_{No}(f) df = \frac{2 \cdot (10^{-6})^2 \cdot (160 \cdot 10^3)^3}{3 \cdot 2 \cdot 10^9} = 1,37 \cdot 10^{-6} \text{ W}$$

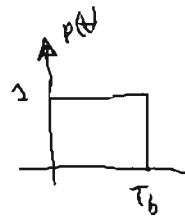
$$P_{S_0}^{\text{Total}} = SNR_0 \cdot P_{No}^{\text{Total}} = 57,8 \text{ mW}$$

$$P_{S_0}^{\text{CANAL}} = P_{S_0}^{\text{Total}} / 40 = 1,45 \text{ mW}$$

$$SNR_0^{\text{CANAL 40}} = \frac{1,45 \cdot 10^{-3}}{9,99 \cdot 10^{-8}} = 14,515 = 41,62 \text{ dB} > 40 \text{ dB}$$

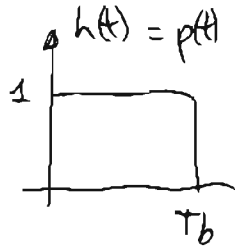
PROBLEMA 2:

Simbolos $g(t) = \pm A p(t)$ con

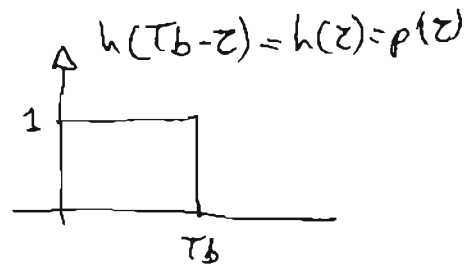


(a) $x(t) = g(t) + w(t)$

$$y(t) = \int_{-\infty}^{\infty} x(z) h(t-z) dz = \int_0^{T_b} x(z) h(t-z) dz$$



$$y(T_b) = \int_0^{T_b} x(z) h(T_b - z) dz$$



$$= \int_0^{T_b} x(z) dz = \int_0^{T_b} g(z) dz + \int_0^{T_b} w(z) dz$$

Si se transmitió 1, $y(T_b)$ es una variable aleatoria Gaussiana

con media y varianza:

$$y(T_b)/1 = A \int_0^{T_b} dz + \int_0^{T_b} w(z) dz = AT_b + \int_0^{T_b} w(t) dt$$

$$E[y(T_b)/1] = AT_b + E\left[\int_0^{T_b} w(t) dt\right] = AT_b + \int_0^{T_b} E[w(t)] dt = AT_b$$

$$\sigma_{y(T_b)/1}^2 = E\left[\left(\int_0^{T_b} w(t) dt\right)^2\right] = E\left[\int_0^{T_b} \int_0^{T_b} w(t) w(z) dt dz\right] =$$

$$= \int_0^{T_b} \int_0^{T_b} \underbrace{E[w(t) w(z)]}_{R_w(t-z)} dt dz = \int_0^{T_b} \int_0^{T_b} R_w(t-z) dt dz$$

por ser ruido blanco:

$$S_W(f) = \frac{N_0}{2} \quad \Leftrightarrow \quad R_W(\tau) = \frac{N_0}{2} \delta(\tau)$$

$$S_W(t-\tau) = \frac{N_0}{2} \delta(t-\tau)$$

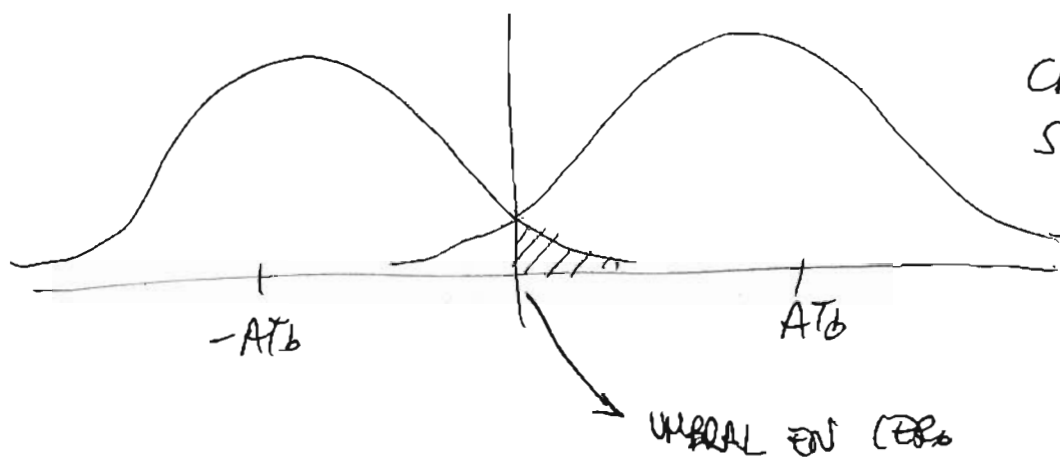
$$\boxed{\sigma^2_{y(T_b)/\phi} = \frac{N_0}{2} \int_0^{T_b} \int_0^{T_b} \delta(t-\tau) d\tau dt = \frac{N_0}{2} \int_0^{T_b} dt = \frac{N_0 T_b}{2}}$$

Si se transmite cero, se puede comprobar que

$$\boxed{E[y(T_b)/\phi] = -AT_b}$$

y

$$\boxed{\sigma^2_{y(T_b)/\phi} = \frac{N_0 T_b}{2}}$$



$$\boxed{P_0 = P_{0\phi} = P_{e1} = \int_0^{\infty} f(y(T_b)/\phi) dy = \frac{1}{\frac{\sqrt{\pi} N_0 T_b}{2}} \int_0^{\infty} \exp\left(-\frac{(y+AT_b)^2}{\frac{2 N_0 T_b}{2}}\right) dy}$$

$$= \frac{1}{\sqrt{\pi} N_0 T_b} \int_0^{\infty} \exp\left(-\frac{(y+AT_b)^2}{N_0 T_b}\right) dy \quad \left| \begin{array}{l} z = \frac{y+AT_b}{\sqrt{N_0 T_b}} \\ dz = \frac{dy}{\sqrt{N_0 T_b}} \end{array} \right.$$

$$= \frac{1}{\sqrt{\pi}} \int_{\frac{AT_b}{\sqrt{N_0 T_b}}}^{\infty} \exp(-z^2) dz = \frac{1}{2} \operatorname{erfc}\left(\frac{AT_b}{\sqrt{N_0 T_b}}\right) = \frac{1}{2} \operatorname{erfc}\left(A \sqrt{\frac{T_b}{N_0}}\right)$$

PROBLEMA 2 (CONTINUACION)

Conocemos todos los datos excepto T_b .

$$10^{-5} = P_e = \frac{1}{2} \operatorname{erfc}(u) \approx \frac{1}{2} \frac{\exp(-u^2)}{u\sqrt{\pi}}$$

$$\frac{\exp(-u^2)}{u} = 2\sqrt{\pi} \cdot 10^{-5} = 3.545 \cdot 10^{-5}$$

u	$\exp(-u^2)/u$
2	$9.15 \cdot 10^{-3}$
3	$4.11 \cdot 10^{-5}$
3,5	$1.367 \cdot 10^{-6}$
3,25	$7.96 \cdot 10^{-6}$
3,12	$1.898 \cdot 10^{-5}$
3,05	$2.99 \cdot 10^{-5}$
3,03	$3.399 \cdot 10^{-5}$
3,02	$3.62 \cdot 10^{-5}$
3,025	$3.51 \cdot 10^{-5}$
3,022	$3.577 \cdot 10^{-5}$

$$u = A \cdot \sqrt{\frac{T_b}{N_0}}$$

$$\frac{u^2}{A^2} = \frac{T_b}{N_0} \Rightarrow T_b = \frac{N_0 \cdot u^2}{A^2}$$

$$\frac{1}{T_b} = R_b = \frac{A^2}{N_0 \cdot u^2} = \frac{(10 \cdot 10^3)^2}{5 \cdot 10^{-12} \cdot (3.022)^2}$$

$$R_b = 2.19 \text{ Mbps}$$



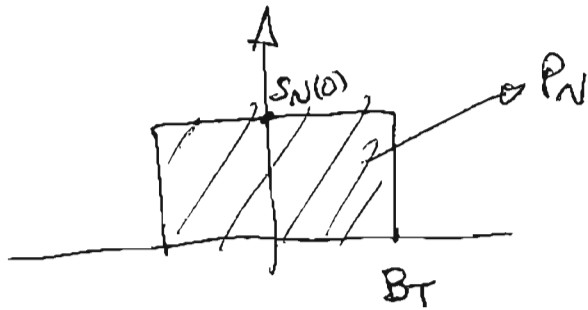
$$S_n(f) = S_w(f) \cdot |H(f)|^2 = \frac{N_0}{2} |H(f)|^2$$

$$h(t) = \operatorname{TT}\left(\frac{t - T_b/2}{T_b}\right) \Leftrightarrow \int_{-T_b/2}^{T_b/2} \operatorname{sinc}\left(\frac{f}{T_b}\right) \cdot \exp(-j2\pi f \frac{T_b}{2})$$

$$S_N(f) = \frac{N_0}{2} T_b^2 \text{sinc}^2(f T_b)$$

$$P_N = \int_{-B_T}^{B_T} S_N(f) df = \frac{N_0 T_b}{2}$$

$$S_N(0) = \frac{N_0 T_b^2}{2}$$



$$S_N(0) \cdot 2 B_T = P_N$$

$$B_T = \frac{P_N}{2 S_N(0)} = \frac{N_0 T_b / 2}{2 \cdot \frac{N_0 T_b^2}{2}} = \frac{1}{2 T_b} = \frac{R_b}{2}$$

$$B_T = 1.095 \text{ MHz}$$